information of multiple types of nodes and links. A snippet of this network is presented in Fig. 1. The blue squares denote different advertisers, green circles denote keywords bought by corresponding advertisers, red circles denote the keyword candidates retrieved from different data sources. The green lines denote the bidding relations between advertisers and keywords, blue lines denote the relations of co-occurring in same auctions between keywords, black lines denote the co-click relations, orange lines denote the adjacent relations in search sessions.
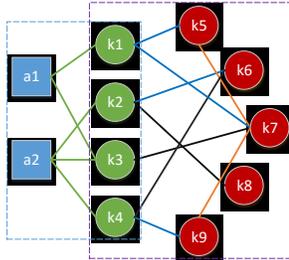
Figure 1: A snippet of this multi-relational network with three types of nodes and four types of relationships.

We collect and sample the data from a commercial search engine in two months to build the complete network, the statistics of this network can be found in Table 1,

Table 1: Information of the datasets

Number of nodes	123713 advertisers, 153291895 keywords
Number of links	211478885 green links, 744963799 blue links, 985014321 black links, 428775103 orange links

3. METHODOLOGY

3.1 Mining Informative Features

For this task, four types of features can be learned as follows,

3.1.1 Meta-Path-Based Similarity Features. Meta-paths [6] can be used to facilitate node proximity measurement in heterogeneous network. We adopt *normalized path count* and *path-constrained random walk* as the similarity features to represent the connectivity between advertisers and keyword candidates along different types of paths. Some possible meta-paths in Fig. 1 are: a1→k3→a2→k2, a1→k1→k5, a1→k3→k7, a1→k1→k7→k5.

3.1.2 Network Embedding Features. Since this multi-relational network is composed of four bipartite networks $\{V_A \cup V_B, E_k\}$ where the keyword vertices are shared across these networks. We can apply the second-order proximity [7] to learn the network embedding features as $min\{-\sum_{k=1\sim4}\sum_{(i,j)\in E_k} w_{ij}.logp(v_i|v_j)\}$, where $p(v_i|v_j) = \exp(\vec{u}_i'^T.\vec{u}_j) / \sum_{k=1}^{|V|} exp(\vec{u}_k'^T.\vec{u}_j)$ denotes the conditional probability of vertex v_i given vertex v_j.

3.1.3 Semantic Features. We use a deep learning neural network model [5] to measure the similarity of candidate keywords and advertiser's original keywords using historical clicked data. A click weighted similarity metric of different pairs of keyword and low-dimension semantic vectors are chosen as features.

3.1.4 Statistical Features. Some other features of advertisers and candidate keywords such as historical impressions and clicks, average cost per click, average post-click quality score, average click-through rate, biding and competition statistics.

3.2 Supervised Link Prediction Model

Based on the informative features mining from multi-relational network. We use the *Field-aware Factorization Machines* model [8] to model and predict if the (advertiser, keyword) pair has a relationship. The FFM model has the form as: $f(X) = w_0 + \sum_{i=1}^{n} w_i x_i + \sum_{i=1}^{n} \sum_{j=i+1}^{n} \left(V_{i,f_j} \times V_{j,f_i}\right) x_i x_j$ and can be trained based on advertisers' historical good bidding keywords and can generate probabilistic score for each candidate keyword.

4. EVALUATION AND CONCLUSIONS

By splitting the dataset into two periods: first month for training and second month for testing, we deploy and verify our approach on the real sponsored search data and compared the top-20 recommendation performance with several existing methods such as random walk (*RW*) and matrix factorization (*MF*) in precision and recall metrics. The performance of different recommendation method is shown in Table 2.

Table 2: Performance of keyword recommendation

Method	Precision	Recall
RW	0.462	0.377
MF	0.535	0.396
SLPM	**0.623**	**0.540**

With rich representation of structure in the multi-relational network and capability of retrieving more candidates, the experimental results demonstrated the effectiveness of proposed approach in recommending suitable keywords to advertisers.

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